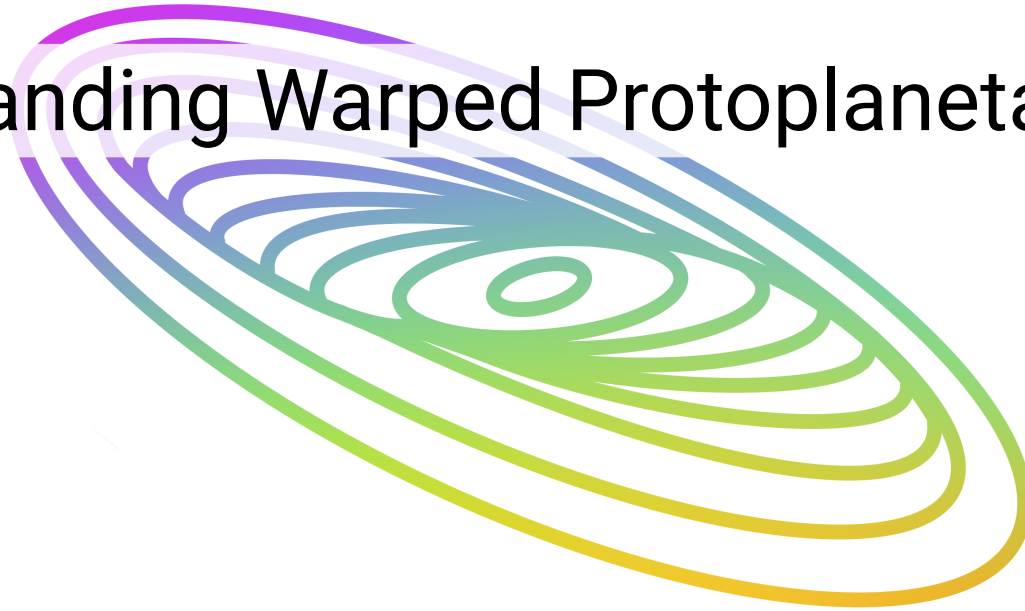


# Inclined to Misalign

## Understanding Warped Protoplanetary Disks



Carolin (Lina) Kimmig  
Postdoc at UniMi  
with Giovanni Rosotti

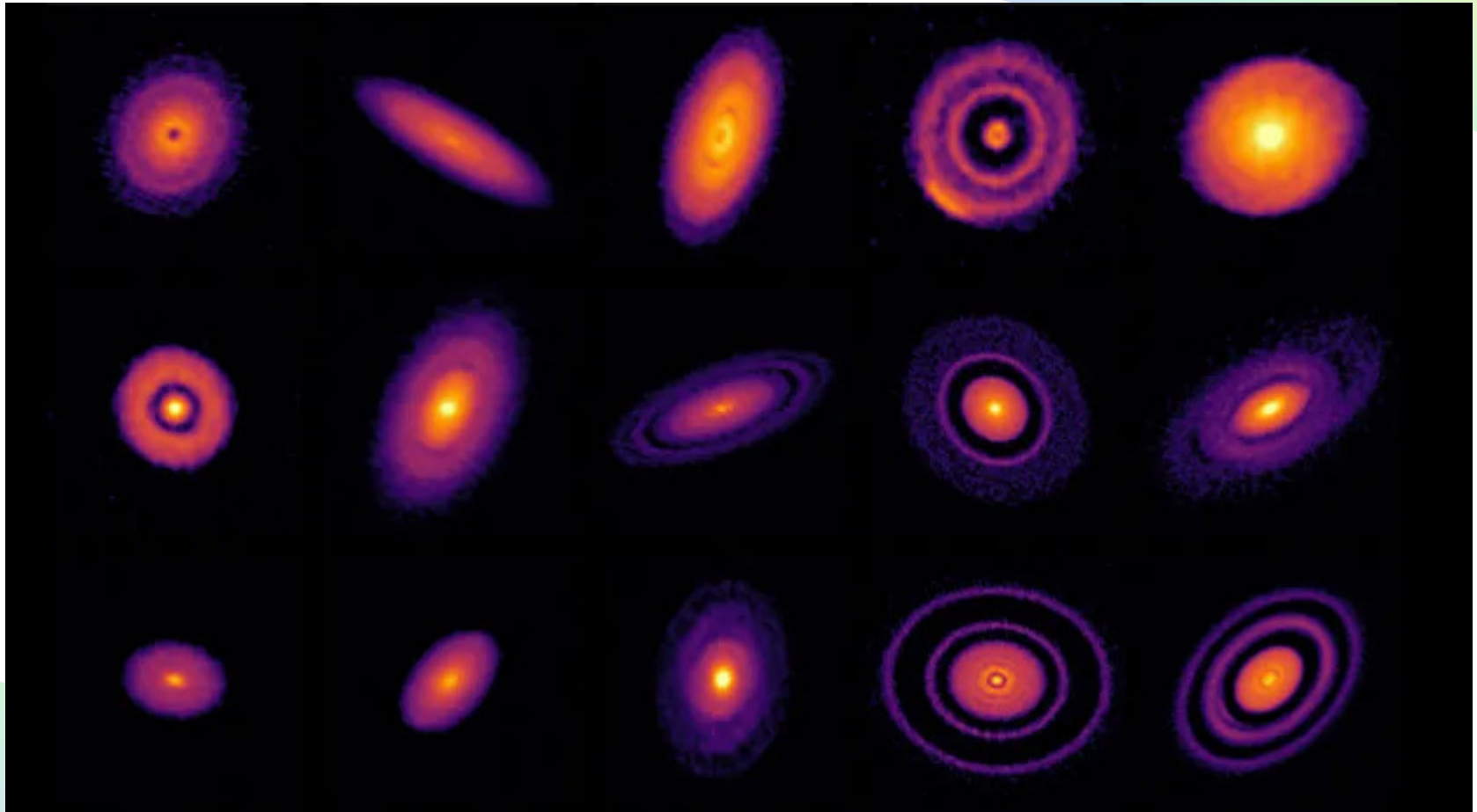
Como Lake centre  
for Astrophysics (CLAP)  
September 11<sup>th</sup> 2025



erc

DFG

Deutsche  
Forschungsgemeinschaft



DSHARP (Andrews et al. 2018)

# Structure

What?

Structure and Formation of Warped Disks

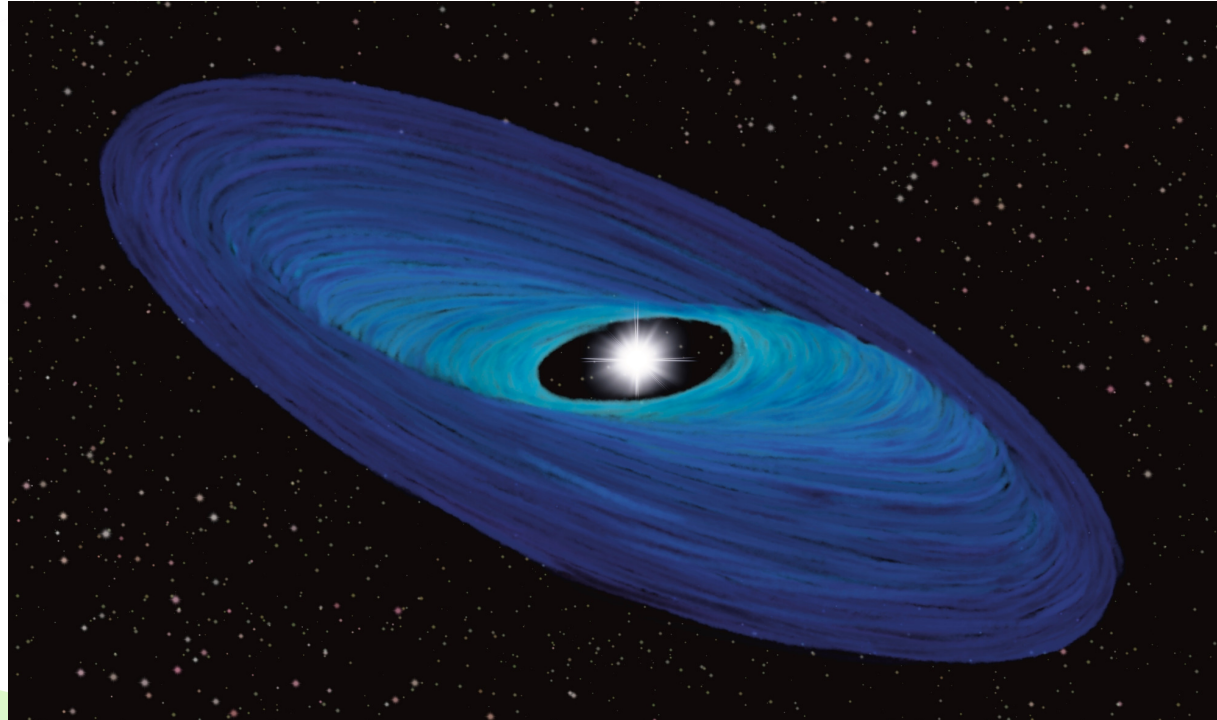
So What?

Observational Evidence

Now What?

Understanding their Dynamics

# What? – Structure of Warped Disks

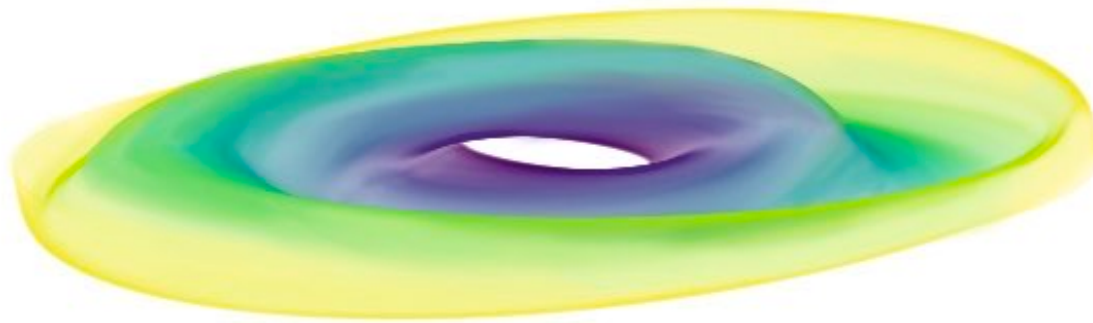


# What? – Structure of Warped Disks

## MWC 758

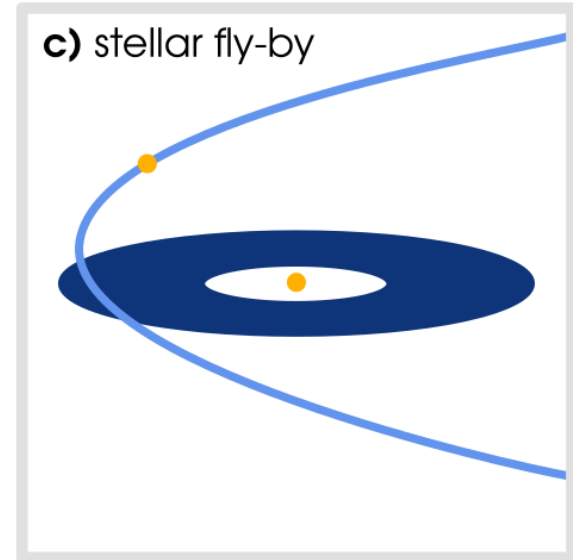
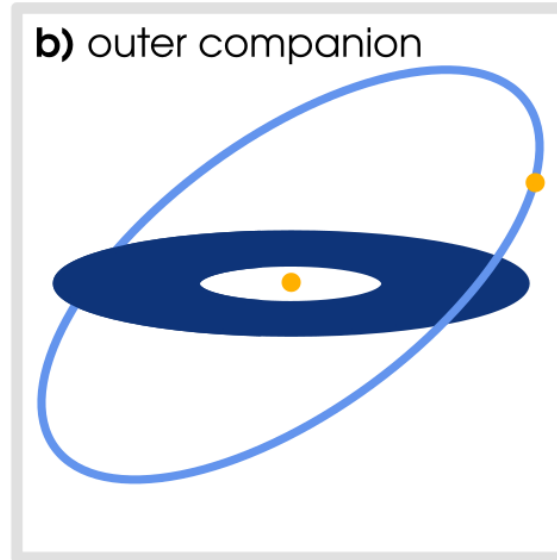
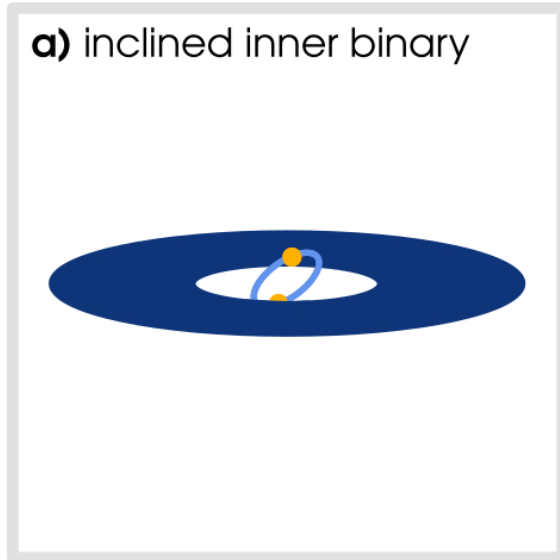
exoALMA

Teague et al. 2025

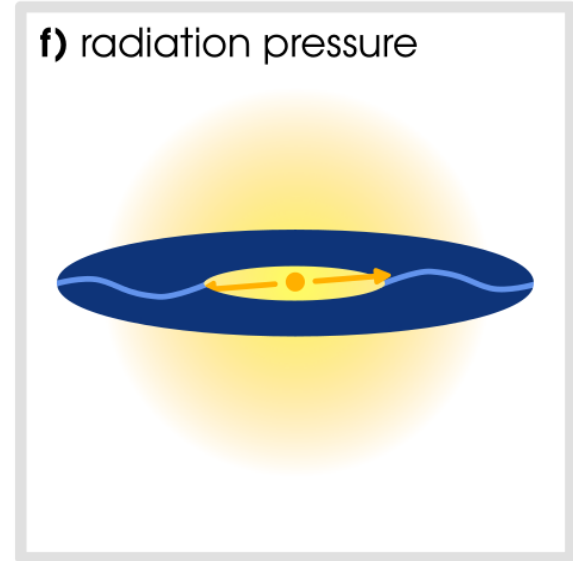
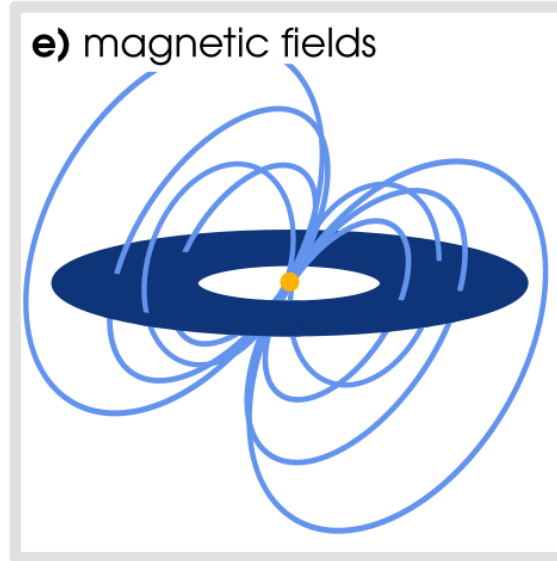


Winter, Benisty, Izquierdo et al. 2025  
ApJL 990 L10 (incl. Lodato, **Kimmig**, Facchini, Rosotti)

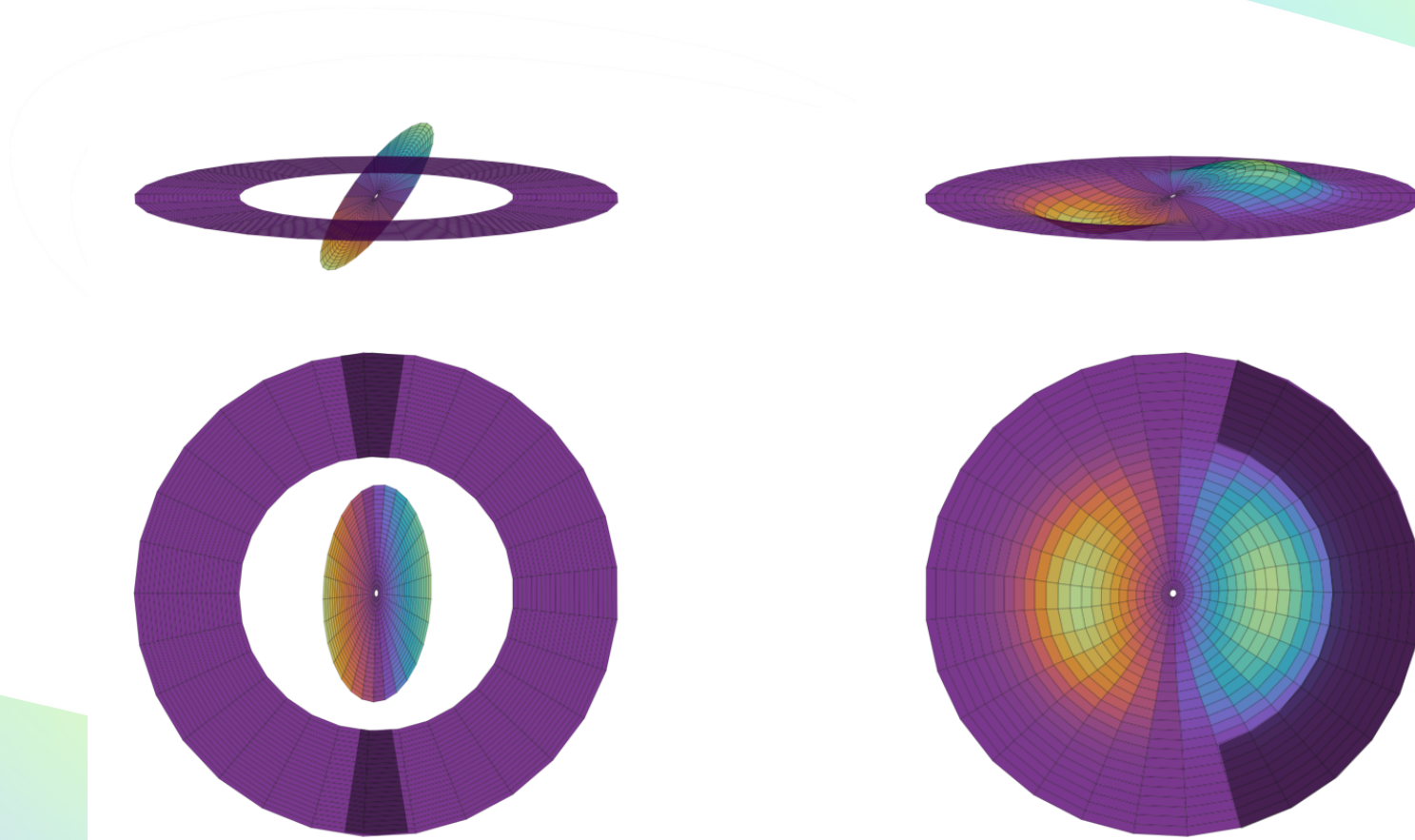
# What? – Formation of Warped Disks



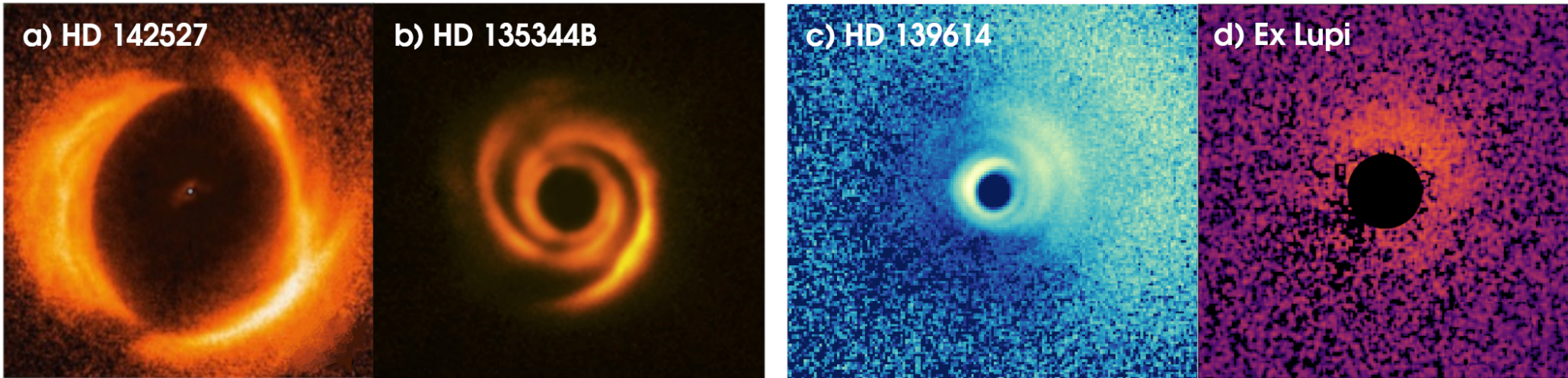
# What? – Formation of Warped Disks



# So What? – Observational Evidence

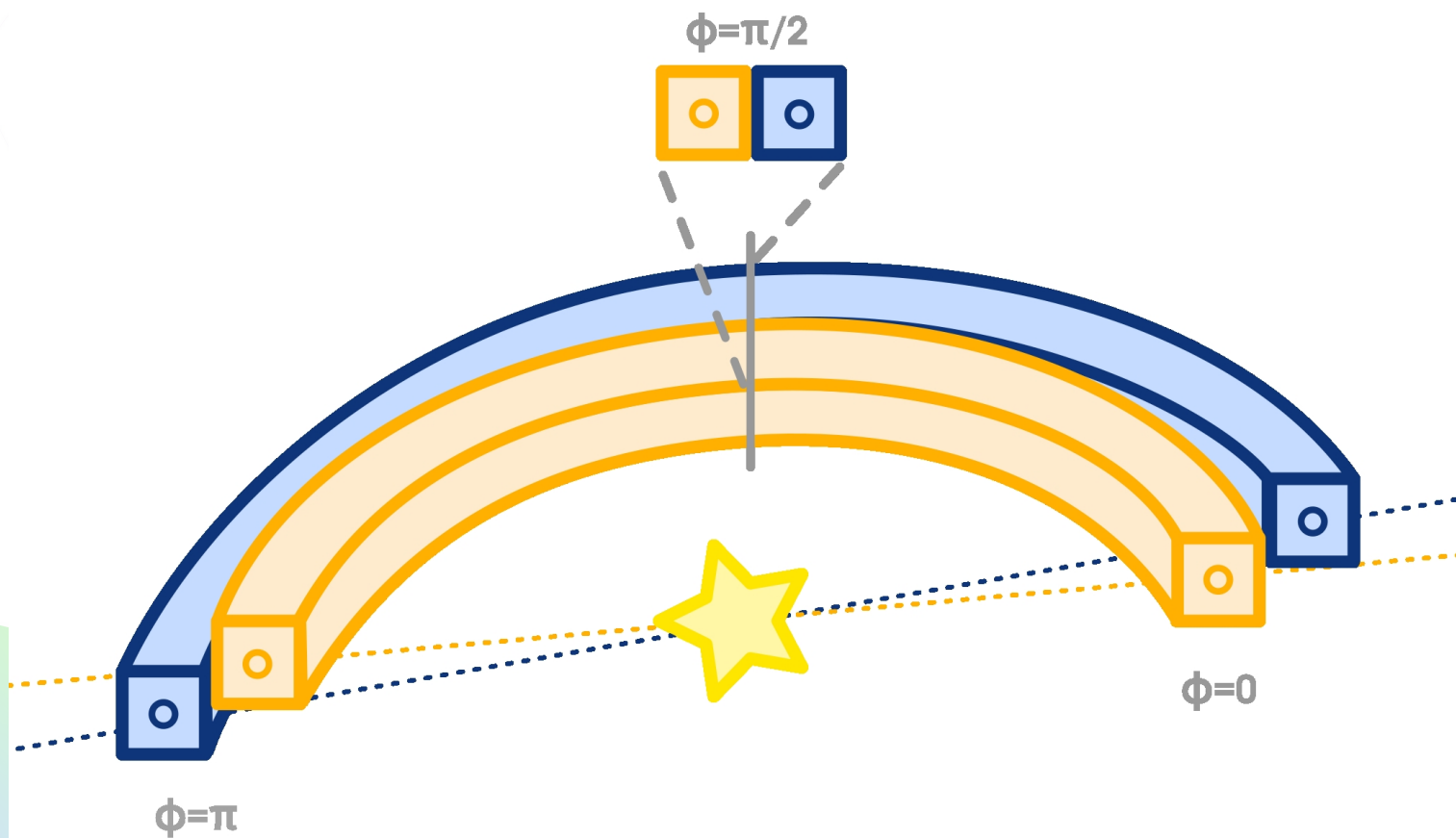


# So What? – Observational Evidence



- a) Avenhaus et al. 2017
- b) Stolker et al. 2016
- c) Muro-Arena et al. 2020
- d) Zurlo et al. 2024

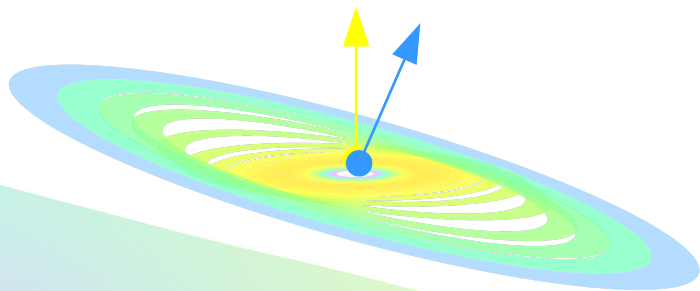
# Now What? – Dynamical Evolution



# Now What? – Dynamical Evolution

$$\frac{\partial \vec{G}}{\partial t} + \omega \vec{l} \times \vec{G} + \alpha \Omega \vec{G} - \left( \vec{l} \times \frac{\partial \vec{l}}{\partial t} \right) \times \vec{G} = \frac{\Sigma H_p^2 r^3 \Omega^3}{4} \frac{\partial \vec{l}}{\partial r} - \frac{3}{2} \alpha \nu \Sigma r^2 \Omega^2 \vec{l}$$

$$\vec{L} = \Sigma r^2 \Omega \vec{l}$$



$$\frac{\partial \Sigma}{\partial t} = -\frac{2}{r} \frac{\partial}{\partial r} \left[ \frac{\frac{\partial \vec{G}}{\partial r} \cdot \vec{l}}{r \Omega} \right]$$

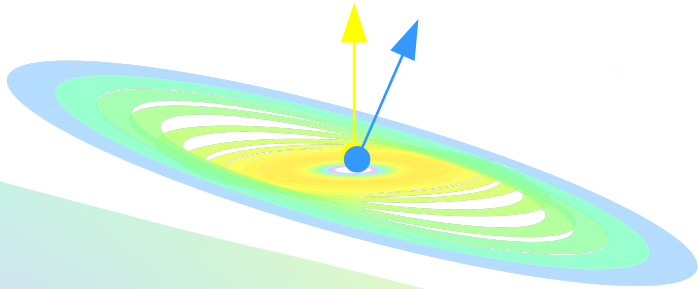
$$\frac{\partial \vec{L}}{\partial t} = -\frac{2}{r} \frac{\partial}{\partial r} \left[ \frac{\frac{\partial \vec{G}}{\partial r} \cdot \vec{l}}{\Sigma r \Omega} \vec{L} \right] + \frac{1}{r} \frac{\partial \vec{G}}{\partial r} + \mathbf{T}.$$

# Now What? – Dynamical Evolution

$$\frac{\partial \vec{G}}{\partial t} + \omega (\vec{l} \times \vec{G}) + \alpha \Omega \vec{G} = \frac{\Sigma H_p^2 r^3 \Omega^3}{4} \frac{\partial \vec{l}}{\partial r}$$

$$\vec{L} = \Sigma r^2 \Omega \vec{l}$$

$$\frac{\partial \vec{L}}{\partial t} = \frac{1}{r} \frac{\partial \vec{G}}{\partial r} + \mathbf{T},$$



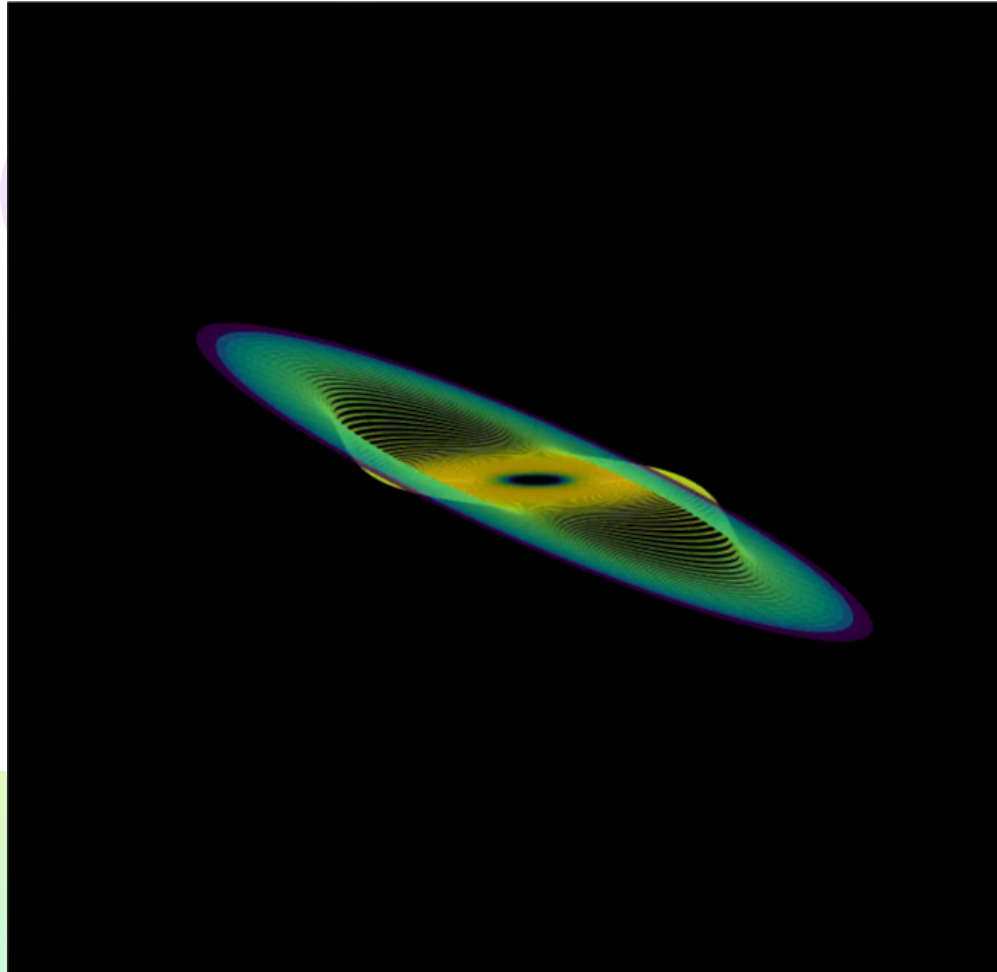
$$\frac{\partial^2 \vec{l}}{\partial t^2} = \frac{1}{\Sigma r^3 \Omega} \frac{\partial}{\partial r} \left( \frac{\Sigma H_p^2 r^3 \Omega^3}{4} \frac{\partial \vec{l}}{\partial r} \right)$$

“pure wave-like equation set”

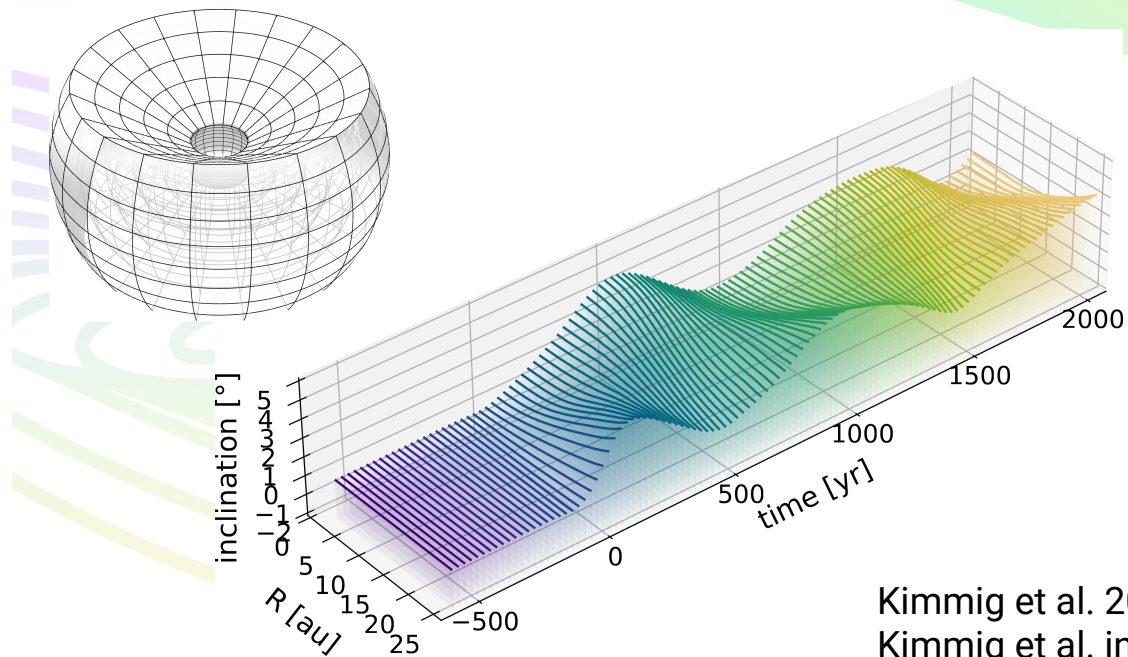
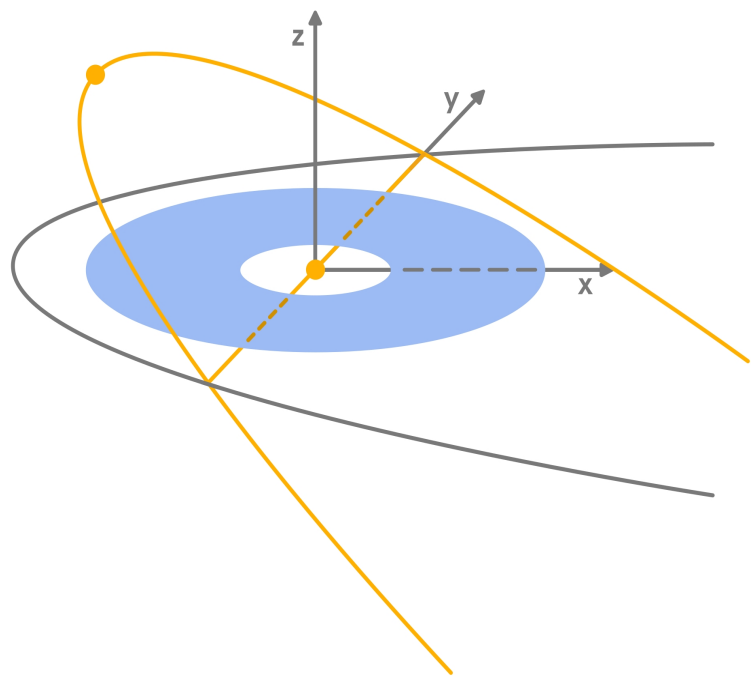
Papaloizou & Lin 1995

Lubow & Ogilvie 2000

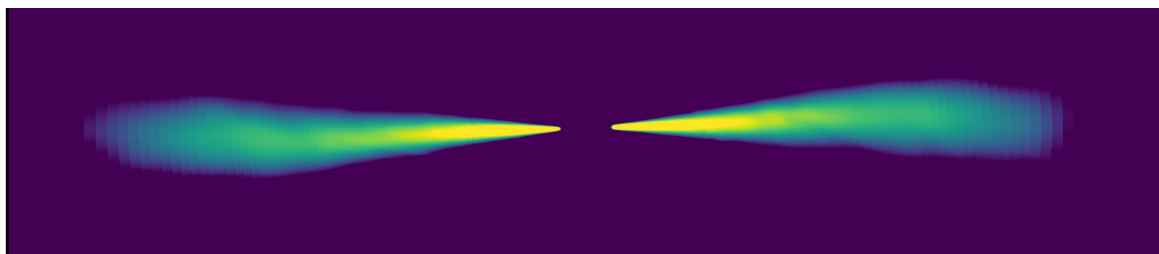
# Now What? – Dynamical Evolution



# Now What? – Modelling Warps in 3D



Kimmig et al. 2024,  
Kimmig et al. in prep.

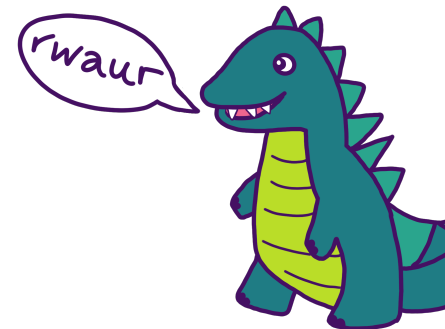
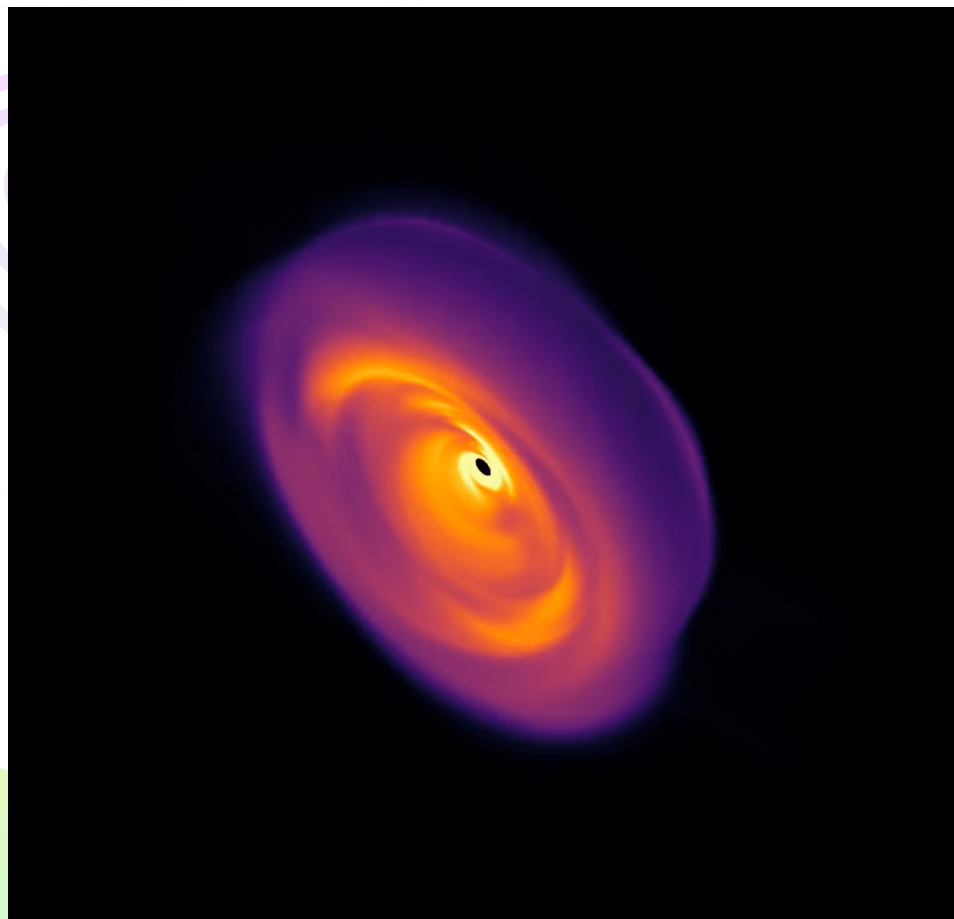


# Now What? – Modelling Warps in 3D

## RW Aur A

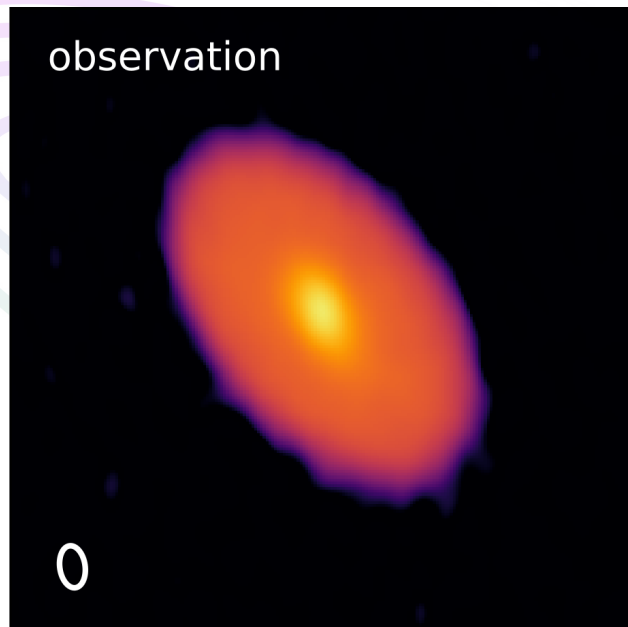
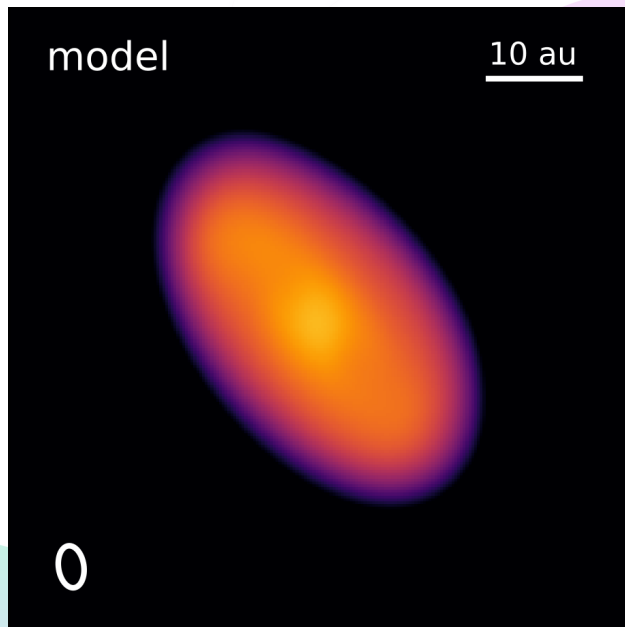
recent close  
encounter  
(300yr ago)

observational  
indications of  
a warp  
(Kurtovic et al. 2024)

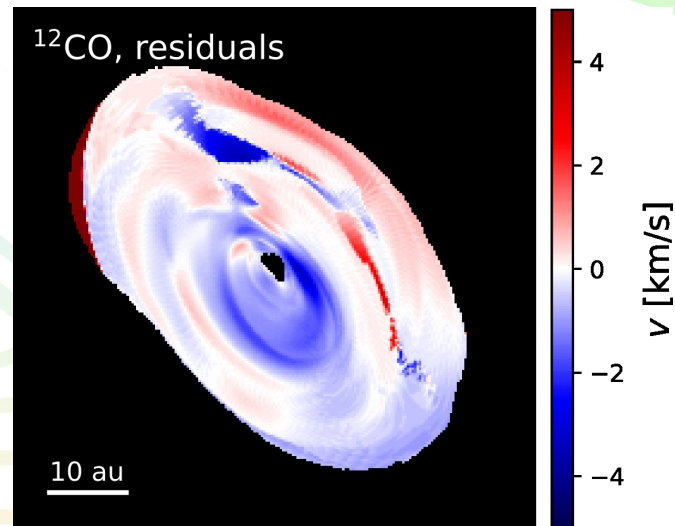


# Now What? – Synthetic Observations

dust continuum



kinematics



RW Aur A

rwaur



# What am I working on?

- Understanding the hydrodynamics of warps in 3D / 1D
- Forming warps in fly-bys
- Warps in disks embedded in turbulent environments
- Linking warp dynamics to observed wiggling jets
- Kinematic signatures to infer warp parameters from observations
- Influence of radiation and cooling on the warp dynamics

# Summary

- Warped protoplanetary disks are **common**
- Warping fundamentally changes the disk **dynamics**
- Theory-observation synergy is key to probing warp **parameters** and determining the **prevalence of warps**